

## Four special values of the (Klein) modular invariant $j$

Suppose that  $j$  is (correctly) normalized with  $j(i) = 1$ , then

$$j\left(\frac{4(5i \pm 1)}{13}\right) = \\ = \left( \frac{(1 - \sqrt{5})^{37}}{2^{39}} \left( 1190448488 - 858585699 \sqrt{2} - 540309076 \sqrt{5} + 374537880 \sqrt{10} + \right. \right. \\ \left. \left. \pm i \sqrt{\sqrt{5}} \left( 693172512 - 595746414 \sqrt{2} - 407357424 \sqrt{5} + 240819696 \sqrt{10} \right) \right) \right)^3,$$

$$j\left(\frac{5(4i \pm 1)}{17}\right) = \\ = \left( \frac{(1 - \sqrt{5})^{37}}{2^{39}} \left( 1190448488 + 858585699 \sqrt{2} - 540309076 \sqrt{5} - 374537880 \sqrt{10} + \right. \right. \\ \left. \left. \pm i \sqrt{\sqrt{5}} \left( 693172512 + 595746414 \sqrt{2} - 407357424 \sqrt{5} - 240819696 \sqrt{10} \right) \right) \right)^3.$$

These special values (along with other values) were derived in my article titled  
"On the Second Memoir of Évariste Galois' Last Letter"